

# GEOMETRY (COMMON CORE)

The University of the State of New York  
REGENTS HIGH SCHOOL EXAMINATION

# GEOMETRY (Common Core)

Thursday, January 26, 2017 — 9:15 a.m. to 12:15 p.m., only

Student Name: \_\_\_\_\_

School Name: \_\_\_\_\_

The possession or use of any communications device is strictly prohibited when taking this examination. If you have or use any communications device, no matter how briefly, your examination will be invalidated and no score will be calculated for you.

Print your name and the name of your school on the lines above.

A separate answer sheet for Part I has been provided to you. Follow the instructions from the proctor for completing the student information on your answer sheet.

This examination has four parts, with a total of 36 questions. You must answer all questions in this examination. Record your answers to the Part I multiple-choice questions on the separate answer sheet. Write your answers to the questions in Parts II, III, and IV directly in this booklet. All work should be written in pen, except for graphs and drawings, which should be done in pencil. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale.

The formulas that you may need to answer some questions in this examination are found at the end of the examination. This sheet is perforated so you may remove it from this booklet.

Scrap paper is not permitted for any part of this examination, but you may use the blank spaces in this booklet as scrap paper. A perforated sheet of scrap graph paper is provided at the end of this booklet for any question for which graphing may be helpful but is not required. You may remove this sheet from this booklet. Any work done on this sheet of scrap graph paper will *not* be scored.

When you have completed the examination, you must sign the statement printed at the end of the answer sheet, indicating that you had no unlawful knowledge of the questions or answers prior to the examination and that you have neither given nor received assistance in answering any of the questions during the examination. Your answer sheet cannot be accepted if you fail to sign this declaration.

Notice...

A graphing calculator, a straightedge (ruler), and a compass must be available for you to use while taking this examination.

DO NOT OPEN THIS EXAMINATION BOOKLET UNTIL THE SIGNAL IS GIVEN.

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## Part I

Answer all 24 questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For each statement or question, choose the word or expression that, of those given, best completes the statement or answers the question. Record your answers on your separate answer sheet. [48]

Use this space for  
computations.

1 Which equation represents the line that passes through the point

$(-2,2)$  and is parallel to  $y = \frac{1}{2}x + 8$ ?

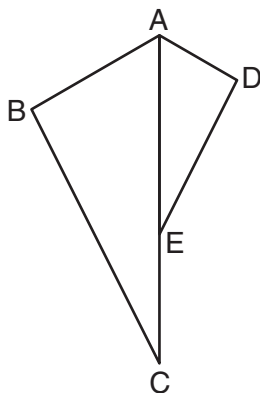
(1)  $y = \frac{1}{2}x$

(3)  $y = \frac{1}{2}x + 3$

(2)  $y = -2x - 3$

(4)  $y = -2x + 3$

2 In the diagram below,  $\triangle ADE$  is the image of  $\triangle ABC$  after a reflection over the line  $AC$  followed by a dilation of scale factor  $\frac{AE}{AC}$  centered at point  $A$ .



Which statement must be true?

(1)  $m\angle BAC = m\angle AED$

(3)  $m\angle DAE = \frac{1}{2}m\angle BAC$

(2)  $m\angle ABC = m\angle ADE$

(4)  $m\angle ACB = \frac{1}{2}m\angle DAB$

3 Given  $\triangle ABC \cong \triangle DEF$ , which statement is *not* always true?

(1)  $\overline{BC} \cong \overline{DF}$

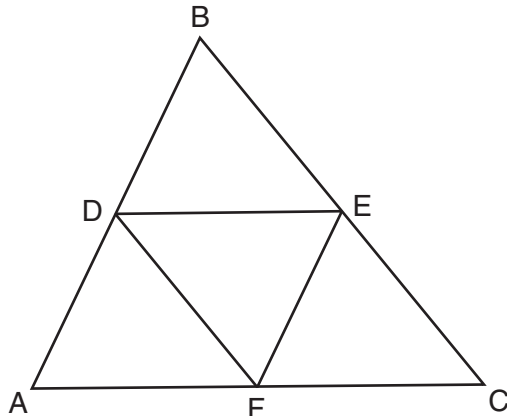
(2)  $m\angle A = m\angle D$

(3) area of  $\triangle ABC =$  area of  $\triangle DEF$

(4) perimeter of  $\triangle ABC =$  perimeter of  $\triangle DEF$

Use this space for computations.

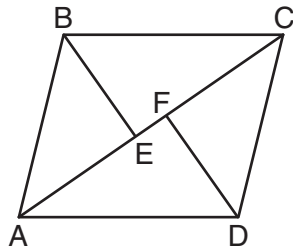
4 In the diagram below,  $\overline{DE}$ ,  $\overline{DF}$ , and  $\overline{EF}$  are midsegments of  $\triangle ABC$ .



The perimeter of quadrilateral  $ADEF$  is equivalent to

- (1)  $AB + BC + AC$
- (2)  $\frac{1}{2}AB + \frac{1}{2}AC$
- (3)  $2AB + 2AC$
- (4)  $AB + AC$

5 In the diagram below, if  $\triangle ABE \cong \triangle CDF$  and  $\overline{AEFC}$  is drawn, then it could be proven that quadrilateral  $ABCD$  is a



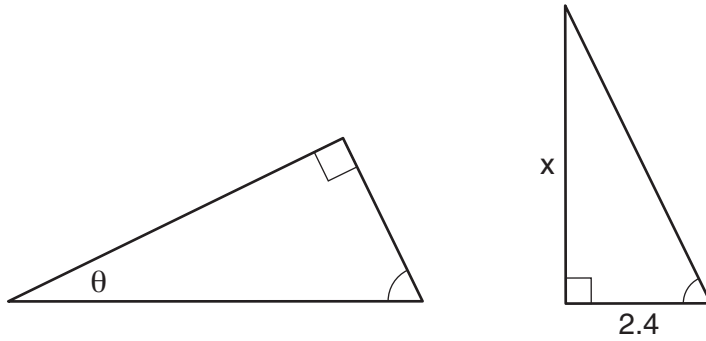
- (1) square
- (2) rhombus
- (3) rectangle
- (4) parallelogram

6 Under which transformation would  $\triangle A'B'C'$ , the image of  $\triangle ABC$ , not be congruent to  $\triangle ABC$ ?

- (1) reflection over the  $y$ -axis
- (2) rotation of  $90^\circ$  clockwise about the origin
- (3) translation of 3 units right and 2 units down
- (4) dilation with a scale factor of 2 centered at the origin

Use this space for computations.

7 The diagram below shows two similar triangles.



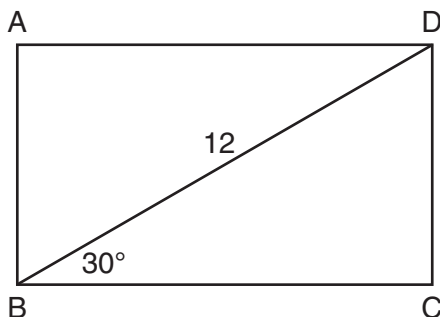
If  $\tan \theta = \frac{3}{7}$ , what is the value of  $x$ , to the *nearest tenth*?

- (1) 1.2
- (2) 5.6
- (3) 7.6
- (4) 8.8

8 A farmer has 64 feet of fence to enclose a rectangular vegetable garden. Which dimensions would result in the biggest area for this garden?

- (1) the length and the width are equal
- (2) the length is 2 more than the width
- (3) the length is 4 more than the width
- (4) the length is 6 more than the width

9 The diagram shows rectangle  $ABCD$ , with diagonal  $\overline{BD}$ .



What is the perimeter of rectangle  $ABCD$ , to the *nearest tenth*?

- (1) 28.4
- (2) 32.8
- (3) 48.0
- (4) 62.4







17 Which rotation about its center will carry a regular decagon onto itself?

- (1)  $54^\circ$  (3)  $198^\circ$   
(2)  $162^\circ$  (4)  $252^\circ$

18 The equation of a circle is  $x^2 + y^2 - 6y + 1 = 0$ . What are the coordinates of the center and the length of the radius of this circle?

- (1) center  $(0,3)$  and radius  $= 2\sqrt{2}$   
(2) center  $(0,-3)$  and radius  $= 2\sqrt{2}$   
(3) center  $(0,6)$  and radius  $= \sqrt{35}$   
(4) center  $(0,-6)$  and radius  $= \sqrt{35}$

19 Parallelogram  $ABCD$  has coordinates  $A(0,7)$  and  $C(2,1)$ . Which statement would prove that  $ABCD$  is a rhombus?

- (1) The midpoint of  $\overline{AC}$  is  $(1,4)$ .  
(2) The length of  $\overline{BD}$  is  $\sqrt{40}$ .  
(3) The slope of  $\overline{BD}$  is  $\frac{1}{3}$ .  
(4) The slope of  $\overline{AB}$  is  $\frac{1}{3}$ .

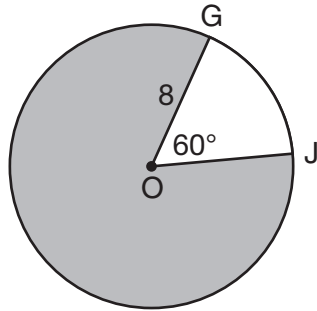
20 Point  $Q$  is on  $\overline{MN}$  such that  $MQ:QN = 2:3$ . If  $M$  has coordinates  $(3,5)$  and  $N$  has coordinates  $(8,-5)$ , the coordinates of  $Q$  are

- (1)  $(5,1)$  (3)  $(6,-1)$   
(2)  $(5,0)$  (4)  $(6,0)$



Use this space for  
computations.

- 21 In the diagram below of circle  $O$ ,  $GO = 8$  and  $m\angle GOJ = 60^\circ$ .



What is the area, in terms of  $\pi$ , of the shaded region?

- (1)  $\frac{4\pi}{3}$                       (3)  $\frac{32\pi}{3}$   
(2)  $\frac{20\pi}{3}$                       (4)  $\frac{160\pi}{3}$
- 22 A circle whose center is the origin passes through the point  $(-5,12)$ .  
Which point also lies on this circle?

- (1)  $(10,3)$                       (3)  $(11, 2\sqrt{12})$   
(2)  $(-12,13)$                       (4)  $(-8, 5\sqrt{21})$

- 23 A plane intersects a hexagonal prism. The plane is perpendicular to the base of the prism. Which two-dimensional figure is the cross section of the plane intersecting the prism?

- (1) triangle                      (3) hexagon  
(2) trapezoid                      (4) rectangle

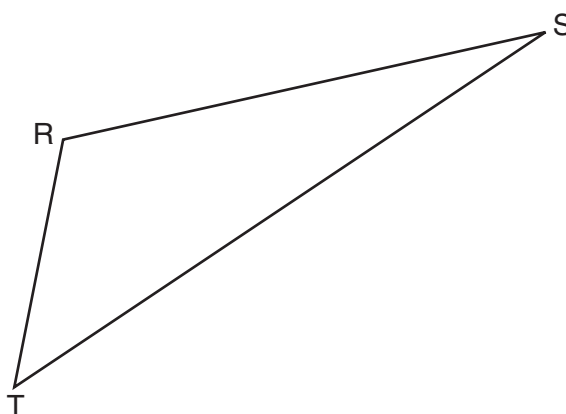
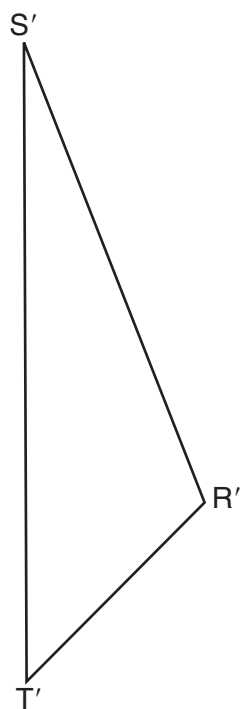
- 24 A water cup in the shape of a cone has a height of 4 inches and a maximum diameter of 3 inches. What is the volume of the water in the cup, to the *nearest tenth of a cubic inch*, when the cup is filled to half its height?

- (1) 1.2                      (3) 4.7  
(2) 3.5                      (4) 14.1

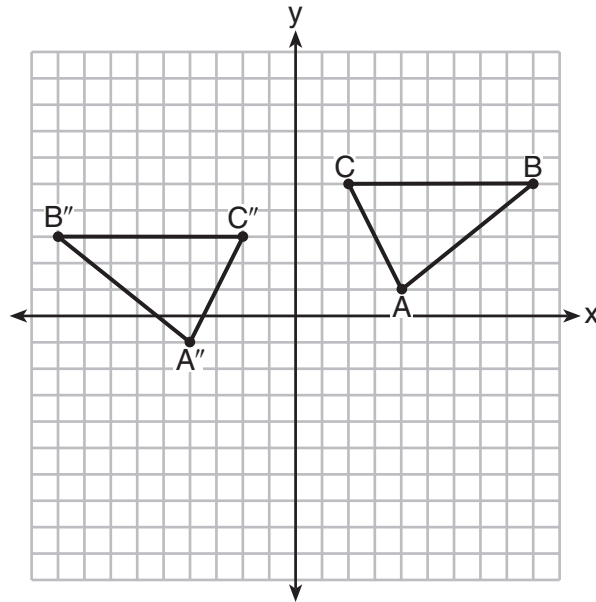
## Part II

Answer all 7 questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [14]

- 25 Using a compass and straightedge, construct the line of reflection over which triangle  $RST$  reflects onto triangle  $R'S'T'$ . [Leave all construction marks.]



26 The graph below shows  $\triangle ABC$  and its image,  $\triangle A''B''C''$ .

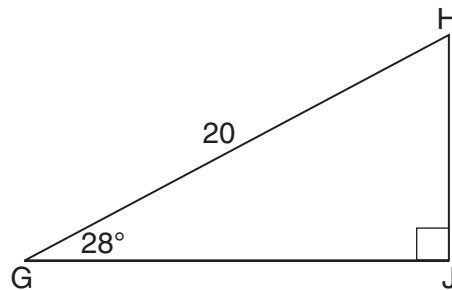


Describe a sequence of rigid motions which would map  $\triangle ABC$  onto  $\triangle A''B''C''$ .

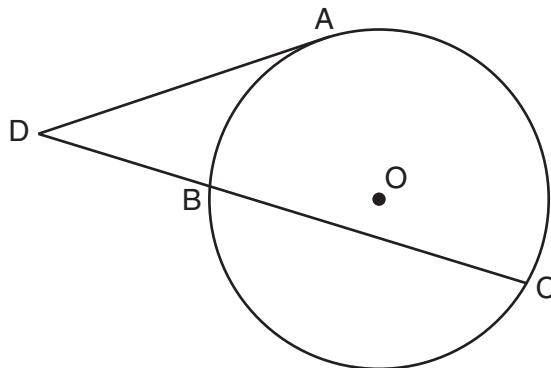
27 When instructed to find the length of  $\overline{HJ}$  in right triangle  $HJG$ , Alex wrote the equation

$\sin 28^\circ = \frac{HJ}{20}$  while Marlene wrote  $\cos 62^\circ = \frac{HJ}{20}$ . Are both students' equations correct?

Explain why.

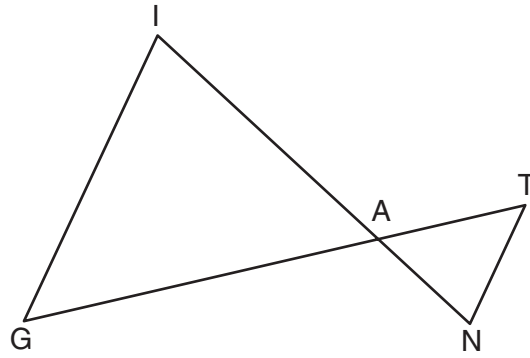


28 In the diagram below, tangent  $\overline{DA}$  and secant  $\overline{DBC}$  are drawn to circle  $O$  from external point  $D$ , such that  $\widehat{AC} \cong \widehat{BC}$ .



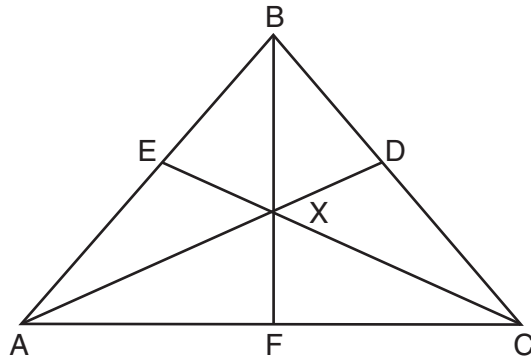
If  $m\widehat{BC} = 152^\circ$ , determine and state  $m\angle D$ .

29 In the diagram below,  $\overline{GI}$  is parallel to  $\overline{NT}$ , and  $\overline{IN}$  intersects  $\overline{GT}$  at A.



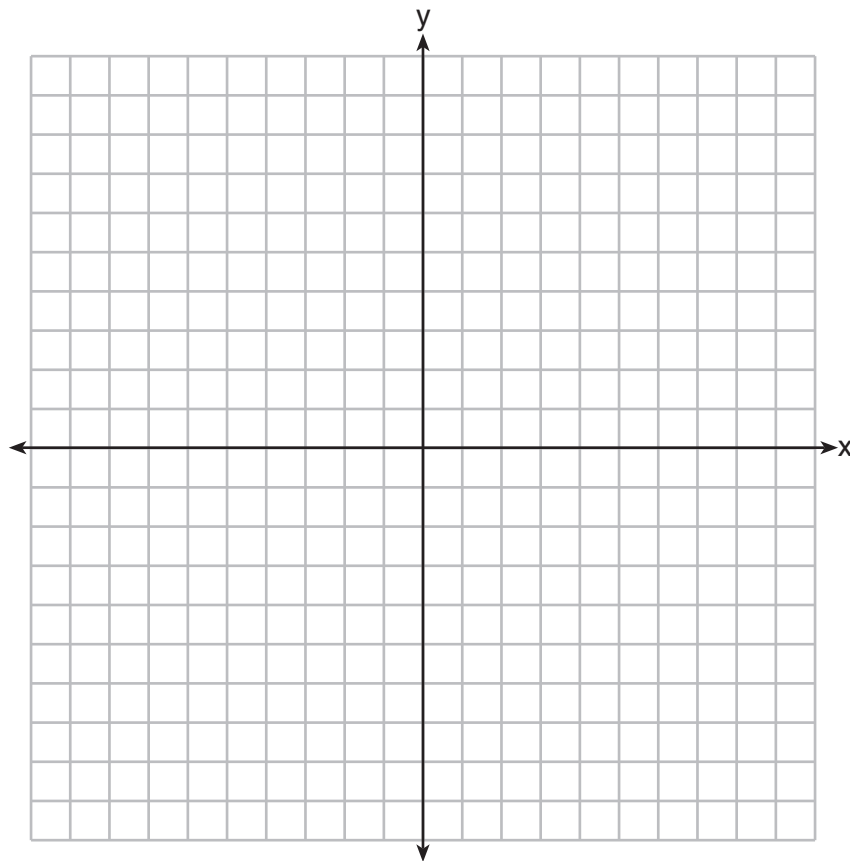
Prove:  $\triangle GIA \sim \triangle TNA$

30 In the diagram below of isosceles triangle  $ABC$ ,  $\overline{AB} \cong \overline{CB}$  and angle bisectors  $\overline{AD}$ ,  $\overline{BF}$ , and  $\overline{CE}$  are drawn and intersect at  $X$ .



If  $m\angle BAC = 50^\circ$ , find  $m\angle AXC$ .

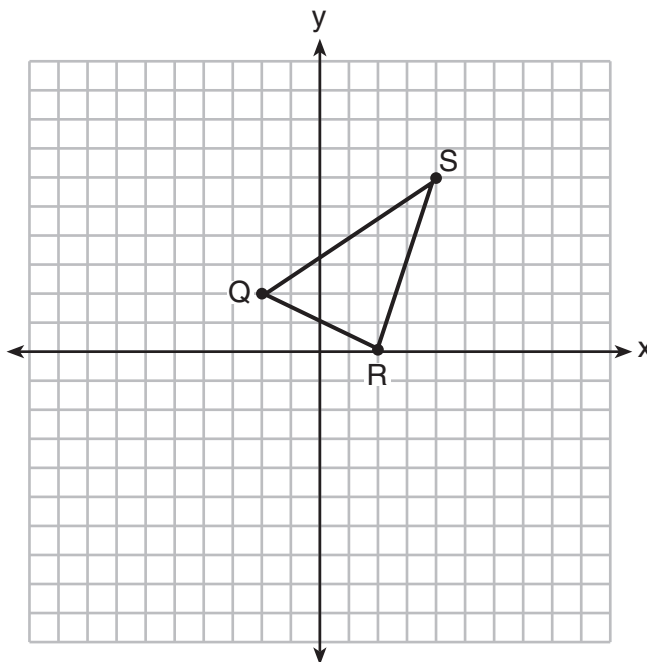
- 31** In square  $GEOM$ , the coordinates of  $G$  are  $(2, -2)$  and the coordinates of  $O$  are  $(-4, 2)$ . Determine and state the coordinates of vertices  $E$  and  $M$ .  
[The use of the set of axes below is optional.]



### Part III

Answer all 3 questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]

32 Triangle  $QRS$  is graphed on the set of axes below.

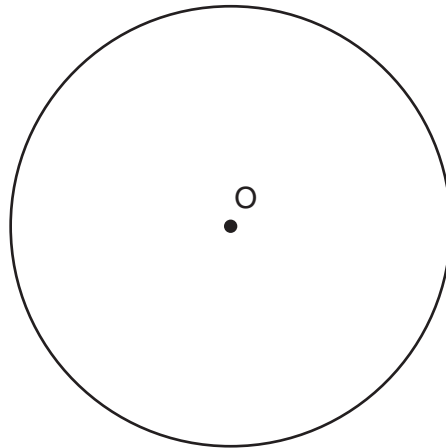


On the same set of axes, graph and label  $\triangle Q'R'S'$ , the image of  $\triangle QRS$  after a dilation with a scale factor of  $\frac{3}{2}$  centered at the origin.

Use slopes to explain why  $\overline{Q'R'} \parallel \overline{QR}$ .



**33** Using a compass and straightedge, construct a regular hexagon inscribed in circle  $O$  below. Label it  $ABCDEF$ . [Leave all construction marks.]



If chords  $\overline{FB}$  and  $\overline{FC}$  are drawn, which type of triangle, according to its angles, would  $\triangle FBC$  be? Explain your answer.

34 A candle maker uses a mold to make candles like the one shown below.

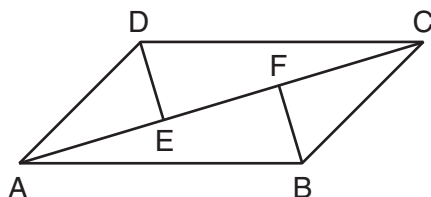


The height of the candle is 13 cm and the circumference of the candle at its widest measure is 31.416 cm. Use modeling to approximate how much wax, to the *nearest cubic centimeter*, is needed to make this candle. Justify your answer.

Part IV

Answer the 2 questions in this part. Each correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. Utilize the information provided for each question to determine your answer. Note that diagrams are not necessarily drawn to scale. For all questions in this part, a correct numerical answer with no work shown will receive only 1 credit. All answers should be written in pen, except for graphs and drawings, which should be done in pencil. [12]

- 35 In quadrilateral  $ABCD$ ,  $\overline{AB} \cong \overline{CD}$ ,  $\overline{AB} \parallel \overline{CD}$ , and  $\overline{BF}$  and  $\overline{DE}$  are perpendicular to diagonal  $\overline{AC}$  at points  $F$  and  $E$ .



Prove:  $\overline{AE} \cong \overline{CF}$

**36** New streetlights will be installed along a section of the highway. The posts for the streetlights will be 7.5 m tall and made of aluminum. The city can choose to buy the posts shaped like cylinders or the posts shaped like rectangular prisms. The cylindrical posts have a hollow core, with aluminum 2.5 cm thick, and an outer diameter of 53.4 cm. The rectangular-prism posts have a hollow core, with aluminum 2.5 cm thick, and a square base that measures 40 cm on each side.

The density of aluminum is  $2.7 \text{ g/cm}^3$ , and the cost of aluminum is \$0.38 per kilogram.

If all posts must be the same shape, which post design will cost the town less?

How much money will be saved per streetlight post with the less expensive design?

**Work space for question 36 is continued on the next page.**

**Question 36 continued**



## High School Math Reference Sheet

1 inch = 2.54 centimeters	1 kilometer = 0.62 mile	1 cup = 8 fluid ounces
1 meter = 39.37 inches	1 pound = 16 ounces	1 pint = 2 cups
1 mile = 5280 feet	1 pound = 0.454 kilogram	1 quart = 2 pints
1 mile = 1760 yards	1 kilogram = 2.2 pounds	1 gallon = 4 quarts
1 mile = 1.609 kilometers	1 ton = 2000 pounds	1 gallon = 3.785 liters
		1 liter = 0.264 gallon
		1 liter = 1000 cubic centimeters

Triangle	$A = \frac{1}{2}bh$
Parallelogram	$A = bh$
Circle	$A = \pi r^2$
Circle	$C = \pi d$ or $C = 2\pi r$
General Prisms	$V = Bh$
Cylinder	$V = \pi r^2 h$
Sphere	$V = \frac{4}{3}\pi r^3$
Cone	$V = \frac{1}{3}\pi r^2 h$
Pyramid	$V = \frac{1}{3}Bh$

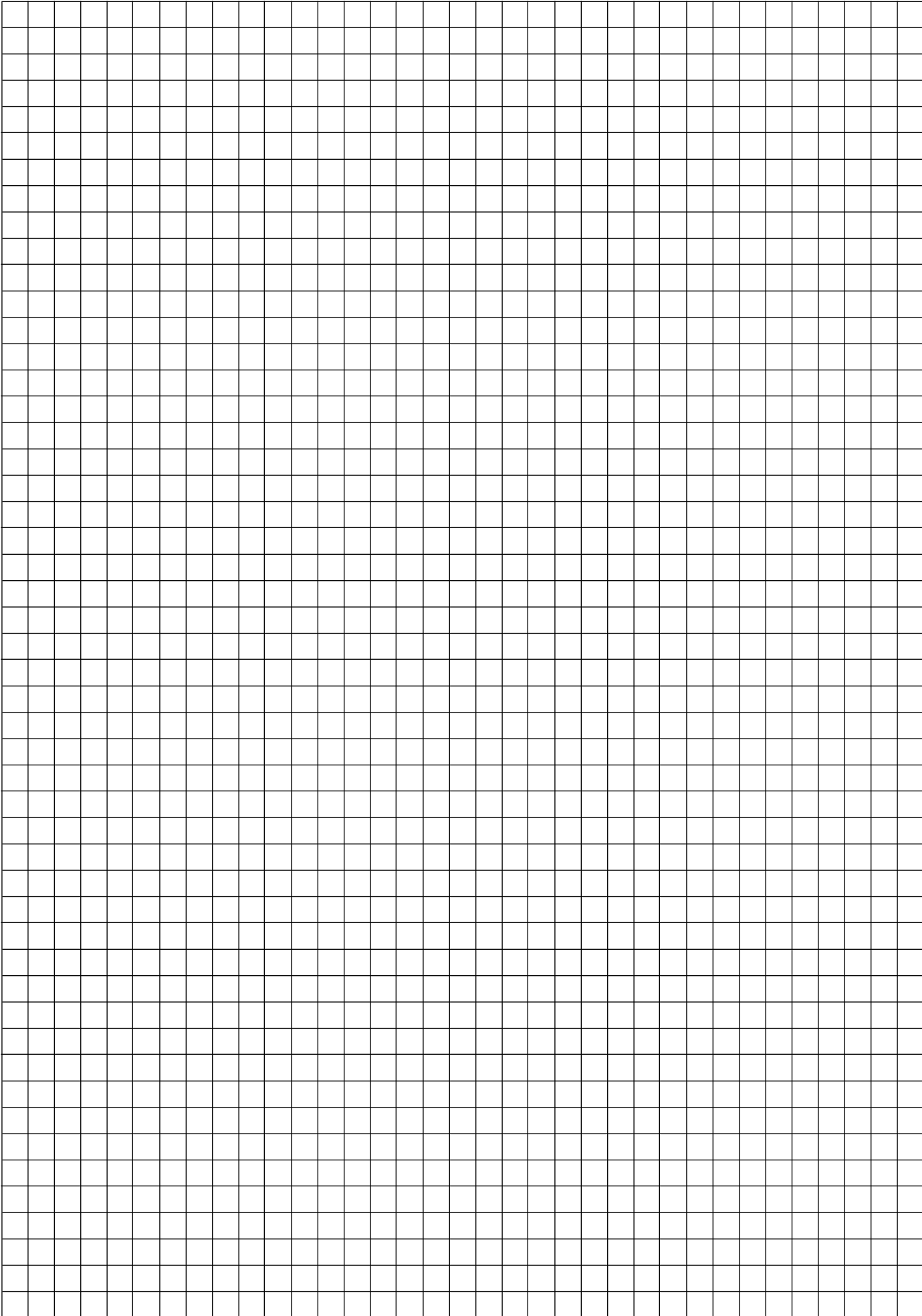
Pythagorean Theorem	$a^2 + b^2 = c^2$
Quadratic Formula	$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
Arithmetic Sequence	$a_n = a_1 + (n - 1)d$
Geometric Sequence	$a_n = a_1 r^{n - 1}$
Geometric Series	$S_n = \frac{a_1 - a_1 r^n}{1 - r}$ where $r \neq 1$
Radians	1 radian = $\frac{180}{\pi}$ degrees
Degrees	1 degree = $\frac{\pi}{180}$ radians
Exponential Growth/Decay	$A = A_0 e^{k(t - t_0)} + B_0$

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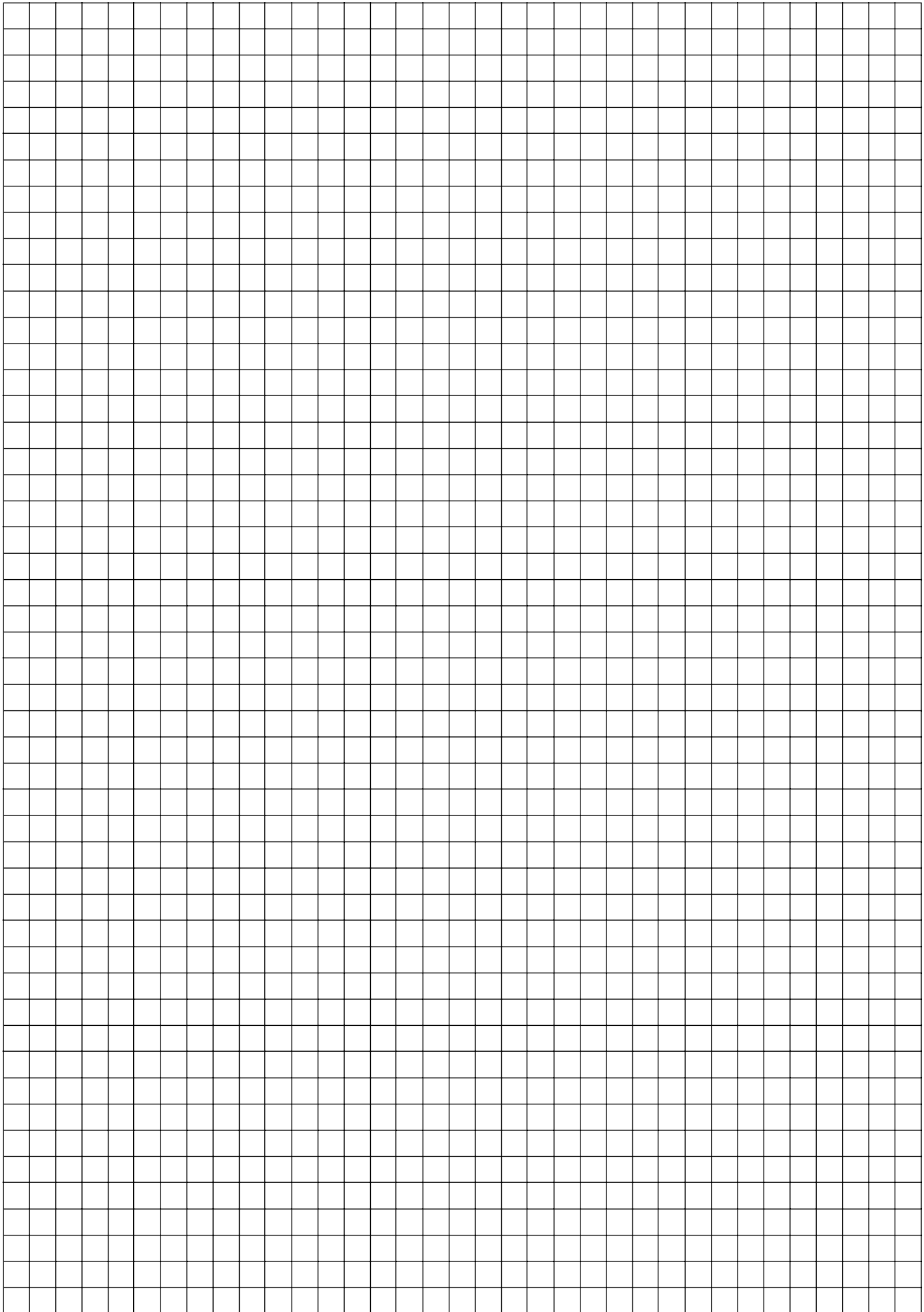
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